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CSE 355

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### Midterm # 2

In the following, assume an alphabet  $\Sigma = \{0, 1\}$  unless stated otherwise. Several questions will use the languages

$$L_1 = \{w \mid w = 0x0\},$$

$$L_2 = \{w \mid w = (01)^i(100)^i; i > 0\},$$

$$L_3 = \{w \mid w = 0^i 1^j 0^i; i, j > 0\},$$

1. Which of these languages is/are regular, context-free, or neither? Explain your answers.

2. Find a PDA for  $L_2$ .

3. Is  $L_1 \cup L_3$  a regular language? a context-free language? Explain your answers.

4. Construct a PDA for  $L_1L_2$ .

5. Suppose you are given a DFA with  $\Sigma = \{0\}$ , states  $\{q_0, q_1, q_2, q_3\}$  with accepting state  $\{q_2\}$  and start state  $q_0$  with transition function  $\delta(q_i, 0) = q_{i+1}$  for  $i = 0, 1, 2$  and  $\delta(q_3, 0) = q_3$ . Can this DFA be minimized? Explain your answer.

6. Let a CFG be given by

$$S \rightarrow AS|\epsilon \quad A \rightarrow AA|B0 \quad B \rightarrow BS|1$$

Is the string 001 in the language generated by this grammar? Explain your answer.

7. Find a CFG for  $L_2^R$ .